

**ΠΑΝΕΛΛΑΔΙΚΕΣ ΕΞΕΤΑΣΕΙΣ**  
**Γ' ΤΑΞΗΣ ΗΜΕΡΗΣΙΟΥ ΓΕΝΙΚΟΥ ΛΥΚΕΙΟΥ**

**ΔΕΥΤΕΡΑ 23 ΜΑΪΟΥ 2016**

**ΕΞΕΤΑΖΟΜΕΝΟ ΜΑΘΗΜΑ: ΦΥΣΙΚΗ**  
**ΠΡΟΣΑΝΑΤΟΛΙΣΜΟΥ (ΝΕΟ ΣΥΣΤΗΜΑ)**

**ΘΕΜΑ Α**

A1) β

A2) γ

A3) β

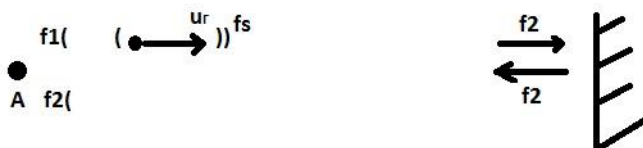
A4) δ

A5) α)Σ β)Λ γ)Σ δ)Λ ε)Λ

**ΘΕΜΑ Β**

B1)

Σωστό το iii



Από το τρένο απευθείας (κιν.πηγή απομακρυνόμενη από ακιν.παρατ.)

$$f_1 = \frac{u_{\eta\chi}}{u_{\eta\chi} + \frac{u_{\eta\chi}}{10}} f_s \Rightarrow f_1 = \frac{10}{11} f_s$$

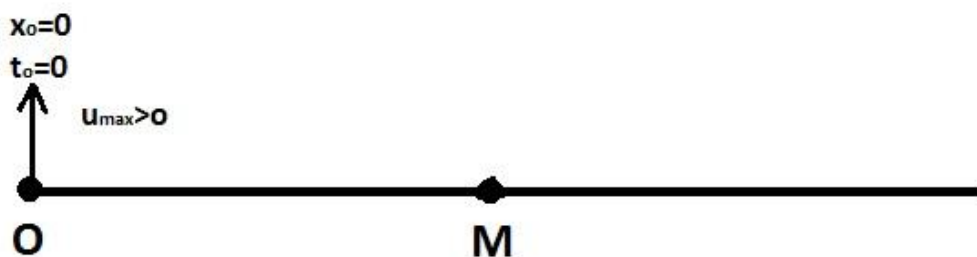
στον βράχο: κιν. πηγή προς ακιν. παρατ.

$$f_2 = \frac{u_{\eta\chi}}{u_{\eta\chi} - \frac{u_{\eta\chi}}{10}} f_s \Rightarrow f_2 = \frac{10}{9} f_s$$

από ακιν. βράχο προς ακίνητο παρατηρητή δεν αλλάζει η  $f_2$

άρα  $\frac{f_1}{f_2} = \frac{9}{11}$  σωστό το iii

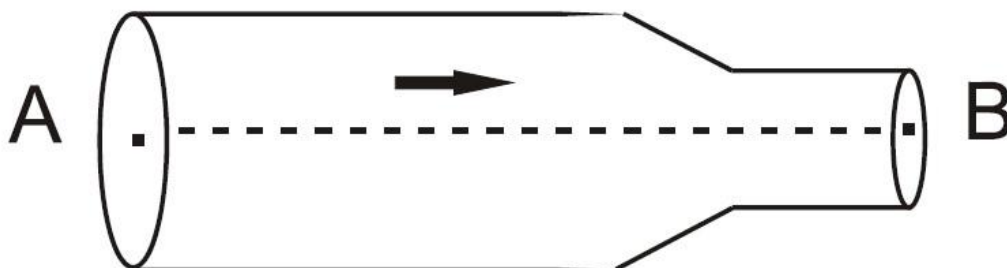
**B2)**



$$\begin{aligned}
 |A'_M| &= |2A \sigma \nu \frac{2\pi x}{\lambda}| = |2A \sigma \nu \frac{2\pi \frac{9\lambda}{8}}{\lambda}| = 2A \sigma \nu \frac{2\pi \cdot 9\lambda}{8\lambda} = \\
 &= 2A \sigma \nu \frac{9\pi}{4} = 2A |\sigma \nu \nu \left( \frac{8\pi + \pi}{4} \right)| = 2A \sigma \nu \nu \left( 2\pi + \frac{\pi}{4} \right) = \\
 &= 2A \sigma \nu \frac{\pi}{4} = 2A \frac{\sqrt{2}}{2} = A\sqrt{2}
 \end{aligned}$$

$$v_{M \max} = \omega \cdot |A'_M| = \frac{2\pi}{T} \cdot A\sqrt{2} \quad (i)$$

**B3)**



$$A_A = 2A_B \quad \frac{1}{2} \rho u_A^2 = \Lambda$$

$$\begin{aligned}
 \Pi_A = \Pi_B &\Rightarrow v_A \cdot A_A = v_B A_B \Rightarrow v_A 2A_B = v_B A_B \\
 &\Rightarrow v_B = 2v_A
 \end{aligned}$$

Bernoulli

$$P_A + \frac{1}{2} \rho u_A^2 = P_B + \frac{1}{2} \rho u_B^2 \Rightarrow$$

$$P_A + \frac{1}{2} \rho u_A^2 = P_B + \frac{1}{2} \rho 4u_A^2 \Rightarrow$$

$$P_A - P_B = \frac{1}{2} \rho 4u_A^2 - \frac{1}{2} \rho u_A^2 \Rightarrow$$

$$P_A - P_B = 3 \cdot \frac{1}{2} \rho u_A^2 \Rightarrow$$

$$P_A - P_B = 3\Delta$$

σωστή (ii)

### ΘΕΜΑ Γ

Γ1)

$$\Theta\text{ΜΚΕ: } K_{\Gamma} - K_A = W_{W_1} + W_N \Rightarrow$$

$$\frac{1}{2} m_1 v_{\Gamma}^2 = m_1 g R \Rightarrow v_{\Gamma} = 10 \text{ m/s}$$

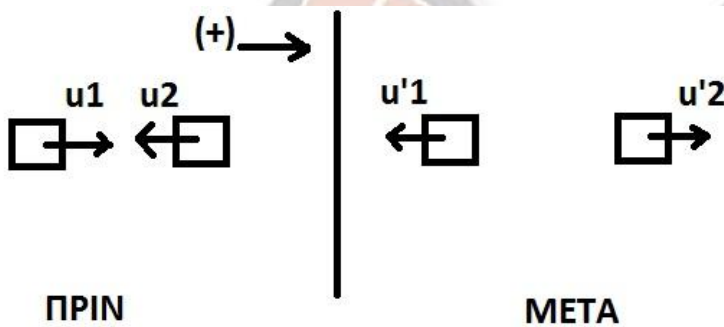
Γ2)

ΘΜΚΕ:  $K_{\Delta} - K_{\Gamma} = W_N + W_N + W_T \Rightarrow$   
 $m_1 \Gamma \rightarrow \Delta$

$$\frac{1}{2} m_1 v_1^2 - \frac{1}{2} m_1 v_{\Gamma}^2 = -\mu m_1 g S_1 \Rightarrow v_1^2 = v_{\Gamma}^2 - 2\mu g S_1 \Rightarrow v_1 = 8 \text{ m/s}$$

$$\left. \begin{aligned} T &= \mu N \\ \Sigma F_y &= 0 \Rightarrow N = w_1 = m_1 g \end{aligned} \right\} \Rightarrow T = \mu m_1 g$$

Από ΑΔΟ και ΑΔΚΕ

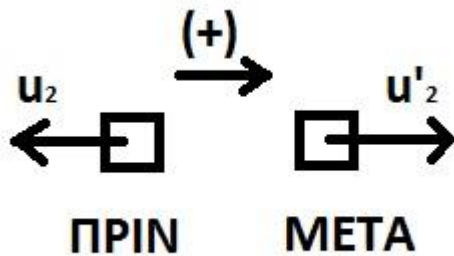


$$-u'_1 = \frac{m_1 - m_2}{m_1 + m_2} u_1 + \frac{2m_2}{m_1 + m_2} (-u_2) \Rightarrow -u'_1 = \frac{-2m_1 u_1}{4m_1} - \frac{6m_1}{4m_1} u_2 \Rightarrow u'_1 = 10 \text{ m/s}$$

$$u'_2 = \frac{2m_1}{m_1 + m_2} u_1 + \frac{m_2 - m_1}{m_1 + m_2} (-u_2) \Rightarrow u'_2 = \frac{2m_1}{4m_1} u_1 - \frac{2m_1}{4m_1} u_2 \Rightarrow u'_2 = 2 \text{ m/s}$$

Άρα  $u'_1 = 10 \text{ m/s}$  ,  $u'_2 = 2 \text{ m/s}$   
 αριστερά , δεξιά

Γ3)



$$\Delta \vec{p}_2 = \vec{p}'_2 - \vec{p}_2$$

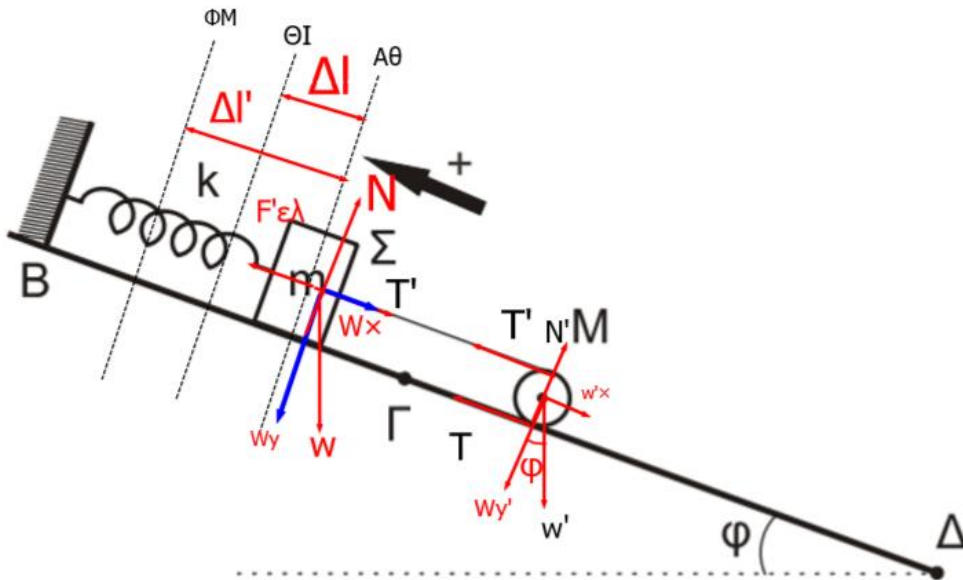
$$\Delta p_2 = m_2 u'_2 - (-m_2 u_2) = m_2 (u'_2 + u_2) = 18 \text{ kg} \frac{\text{m}}{\text{s}}$$

Φορά δεξιά

Γ4)

$$\begin{aligned} \Delta K_1 \% &= \frac{K'_1 - K_1}{K_1} \cdot 100 = \left( \frac{K'_1}{K_1} - 1 \right) \cdot 100 = \\ &= \left( \frac{\frac{1}{2} m_1 u_1'^2}{\frac{1}{2} m_1 u_1^2} - 1 \right) \cdot 100 = \frac{36}{64} \cdot 100 \Rightarrow 56,25\% \end{aligned}$$

**ΘΕΜΑ Δ**



**Δ1)**

κυλ.  $\Sigma \tau_A = 0 \Rightarrow Mg\eta\mu\phi\mathcal{R} - T'2\mathcal{R} = 0 \Rightarrow T' = \frac{Mg\eta\mu\phi}{2} = 5\text{N}$

m:  $\Sigma F_x = 0 \Rightarrow T' + mg\eta\mu\phi - F'_{ελ} = 0 \Rightarrow$

$F'_{ελ} = T' + mg\eta\mu\phi \Rightarrow F'_{ελ} = 10\text{N}$

$F'_{ελ} = \kappa \cdot \Delta l \Rightarrow \Delta l' = 0,1\text{m}$

**Δ2)**

Όταν κόβεται το νήμα το σώμα είναι ακίνητο άρα σε Α.Θ. ταλάντωσης.

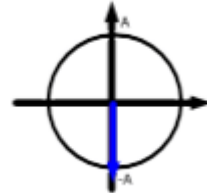
το κέντρο ταλ. είναι:



ΘΙ:  $\Sigma F_x = 0 \Rightarrow F_{ελ} = w_x \Rightarrow \kappa \Delta l = mg \eta \mu \varphi \Rightarrow \Delta l = 0,05m$  από το ΦΜ

Άρα το πλάτος είναι  $A = \Delta l' - \Delta l = 0,05m$

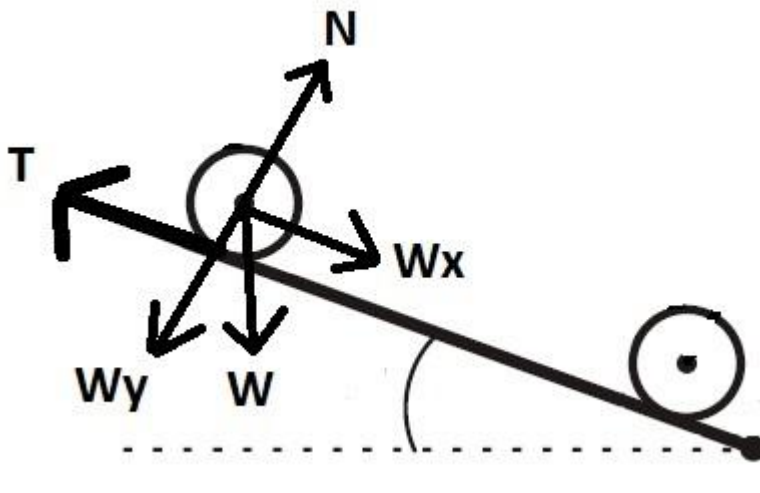
για  $t = 0$   $x = -A \Rightarrow \varphi_0 = \frac{3\pi}{2} \text{rad}$ ,  $\omega = \sqrt{\frac{\kappa}{m}} = 10 \text{rad/s}$



Άρα  $\Sigma F = -kx \Rightarrow \Sigma F = -\kappa A \eta \mu(\omega t + \varphi_0)$

$$\Sigma F = -5\eta \mu\left(10t + \frac{3\pi}{2}\right)$$

Δ3)



ΘΕΕ:



$$K_2 - \cancel{K_1} = W_{w_x} + W_{w_y} + \cancel{W_N} + \cancel{(W_{T_{\mu\epsilon\tau}} + W_{\tau, \sigma\tau\rho})}^{0*} \Rightarrow$$

$$\frac{1}{2} M u_{cm}^2 + \frac{1}{2} \cdot \frac{1}{2} \underbrace{M R^2 \omega^2}_{u_{cm}^2} = M g \eta \mu \varphi \cdot S$$

$$S = \theta \cdot R = 2\pi N R = 2\pi \frac{12}{\pi} \cdot \frac{1}{10} = 2,4 \text{ m}$$

$$\text{Άρα: } \frac{3}{4} R^2 \omega^2 = g \eta \mu \varphi \cdot S \Rightarrow \frac{3}{4} \omega^2 \cdot \frac{1}{100} = 10 \cdot \frac{1}{2} \cdot 2,4 = 12$$

$$\omega^2 = 1600 \Rightarrow \omega = 40 \text{ rad / s}$$

$$L = I_{cm} \cdot \omega = \frac{1}{2} M R^2 \cdot \omega = \frac{1}{2} \cdot 2 \cdot \frac{1}{100} \cdot 40 = 0,4 \text{ kg} \frac{\text{m}^2}{\text{s}}$$

$$\left. \begin{array}{l} *W_T = -T\Delta x \\ W_{\tau, \sigma\tau\rho} = TR\Delta\theta = T\Delta x \end{array} \right\} W_{\tau, \sigma\tau\rho} = 0$$

Δ4)

$$\begin{aligned} \frac{dK_{ολ}}{dt} &= \frac{dK_{\mu\epsilon\tau}}{dt} + \frac{dK_{\sigma\tau\rho}}{dt} = \Sigma F \cdot u_{cm} + \Sigma \tau \cdot \omega \\ &= (w_X - T) u_{cm} + TR\omega \\ &= w_X u_{cm} - T u_{cm} + T u_{cm} \\ &= M g \eta \mu \varphi \cdot u_{cm} \end{aligned}$$

2<sup>ος</sup> Ν.Ν. μετ

$$\left. \begin{aligned} Mg\eta\mu\varphi - T &= M\alpha_{cm} \\ T \cdot R &= \frac{1}{2} MR^2 \frac{\alpha_{cm}}{R} \end{aligned} \right| \Rightarrow Mg\eta\mu\varphi = \frac{3}{2} Ma_{cm}$$

ΘΝΣΚ. στρ.

$$\alpha_{cm} = \frac{2}{3} g\eta\mu\varphi$$

$$\alpha_{cm} = \frac{10}{3} m/s^2$$

Κ.χ. ολ.  $\alpha_{\gamma} = \frac{\alpha_{cm}}{R}$

$$u_{cm} = \alpha_{cm} \cdot t = 10 m/s$$

Άρα  $\frac{dK_{ολ}}{dt} = 100 \text{ Watt } (j/s)$

**Επιμέλεια**

**Αγγελής Γ.**

**Δοξόπουλος Κ.**