

**ΠΑΝΕΛΛΑΔΙΚΕΣ ΕΞΕΤΑΣΕΙΣ
Δ' ΤΑΞΗΣ ΕΣΠΕΡΙΝΟΥ ΓΕΝΙΚΟΥ ΛΥΚΕΙΟΥ ΚΑΙ ΕΠΑΛ
(ΟΜΑΔΑ Β΄)
ΠΑΡΑΣΚΕΥΗ 29 ΜΑΪΟΥ 2015
ΕΞΕΤΑΖΟΜΕΝΟ ΜΑΘΗΜΑ: ΦΥΣΙΚΗ
ΘΕΤΙΚΗΣ ΚΑΙ ΤΕΧΝΟΛΟΓΙΚΗΣ ΚΑΤΕΥΘΥΝΣΗΣ (ΚΑΙ ΤΩΝ
ΔΥΟ ΚΥΚΛΩΝ)**

ΘΕΜΑ Α

A1. α

A2. β

A3. α

A4. δ

A5. α. Δ

β. Δ

γ. Σ

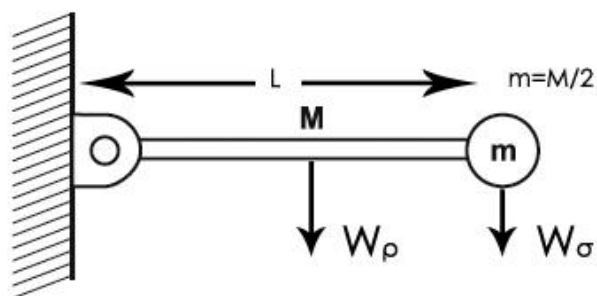
δ. Δ

ε. Σ

ΘΕΜΑ Β

Β1.

(iii) ΣΩΣΤΟ



$$\Sigma \tau_0^{ολικη} = I^{ολικη} \alpha_\gamma \Rightarrow$$

$$\Sigma \tau_0 = \left(\frac{1}{3} ML^2 + \frac{M}{2} L^2 \right) \alpha_\gamma \Rightarrow$$

$$\Sigma \tau_0 = \frac{5}{6} ML^2 \alpha_\gamma \Rightarrow$$

$$Mg \frac{L}{2} + \frac{M}{2} gL = \frac{5}{6} ML^2 \alpha_\gamma \Rightarrow$$

$$\frac{g}{2} + \frac{g}{2} = \frac{5}{6} L \alpha_\gamma \Rightarrow$$

$$g = \frac{5}{6} L \alpha_\gamma \Rightarrow \alpha_\gamma = \frac{6g}{5L}$$

$$\frac{\Delta L_\rho}{\Delta t} = \Sigma \tau_\rho = I_\rho \cdot \alpha_\gamma = \frac{1}{3} ML^2 \alpha_\gamma = \frac{1}{3} ML^2 \frac{6g}{5L} = \frac{2MgL}{5}$$

B2.

(i) ΣΩΣΤΟ

$$\varphi = 2\pi \left(\frac{t}{T} - \frac{x}{\lambda} \right) \rightarrow x = 0 \quad \varphi = 4\pi \text{ rad} \quad \text{άρα } 4\pi = 2\pi \frac{t}{T} \Rightarrow$$

↓

$$\frac{t}{T} = 2 \stackrel{t=2\text{sec}}{\Rightarrow}$$

$$x = 8\text{m} \quad \varphi = 0 \Rightarrow$$

$$\frac{2}{T} = 2 \Rightarrow T = 1\text{sec}$$

$$\varphi = 2\pi \left(\frac{t}{T} - \frac{x}{\lambda} \right) \Rightarrow$$

$$0 = 2\pi \left(2 - \frac{8}{\lambda} \right) \Rightarrow$$

$$2 - \frac{8}{\lambda} = 0 \Rightarrow \frac{8}{\lambda} = 2 \Rightarrow \lambda = 4\text{m}$$

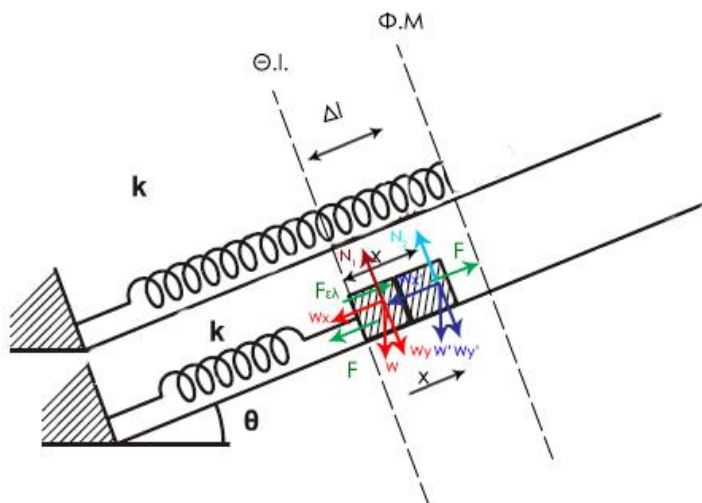
$$\psi = A\eta\mu 2\pi \left(\frac{t}{T} - \frac{x}{\lambda} \right) \Rightarrow$$

Άρα

$$\psi = A\eta\mu 2\pi \left(t - \frac{x}{4} \right)$$

B3.

ΣΩΣΤΟ (i)



$$\Theta\text{Ι σύστημα} : \Sigma F = 0 \Rightarrow F + F_{ελ} - W_{2x} - W_{1x} - F = 0 \Rightarrow$$

$$\Rightarrow k\Delta l = (m_1 + m_2) g \eta \mu \theta$$

$$\Delta l = \frac{(m_1 + m_2) g \eta \mu \theta}{k}$$

$$D_{\text{συστ}} = K = (m_1 + m_2) \omega^2$$

$$\gamma.\alpha.\tau. m_2 : \Sigma F_2 = -D_2 x \Rightarrow$$

$$D_2 = m_2 \omega^2 \Rightarrow D_2 = \frac{m_2 k}{m_1 + m_2} \left| \Rightarrow F - w_{2x} = -D_2 x \Rightarrow F = w_{2x} - D_2 x \right.$$

μη απώλεια επαφής όσο

$$F > 0 \Rightarrow w_{2x} - D_2 x > 0 \Rightarrow w_{2x} > D_2 x \Rightarrow$$

$$m_2 g \eta \mu \theta > \frac{m_2 k}{m_1 + m_2} x \Rightarrow kx < (m_1 + m_2) g \eta \mu \theta \quad \text{ή} \quad x < \Delta l$$

εφόσον έχουμε ταλάντωση με πλάτος Λ θα πρέπει

$$k\Lambda < (m_1 + m_2) g \eta \mu \theta$$

ΘΕΜΑ Γ

Γ1.

$$U_E = E - U_B = E - \frac{1}{2}Li^2 \quad \left| \begin{array}{l} E = 8 \cdot 10^{-2} \text{ J} \\ \frac{1}{2}L = 8 \cdot 10^{-2} \Rightarrow L = 16 \cdot 10^{-2} \text{ H} \end{array} \right.$$

$$U_E = 8 \cdot 10^{-2} - 8 \cdot 10^{-2} i^2$$

$$E = \frac{1}{2}CV^2 \Rightarrow 8 \cdot 10^{-2} = \frac{1}{2}C \cdot 16 \cdot 10^{-2} \Rightarrow C = 10^{-4} \text{ F}$$

$$T = 2\pi\sqrt{LC} = 8\pi \cdot 10^{-3} \text{ s}, \omega = \frac{2\pi}{T} = 250 \text{ rad/s}$$

$$\left. \begin{array}{l} \text{για } t=0 \quad q = CV = 4 \cdot 10^{-3} \text{ C} \\ i = 0 \end{array} \right| \Rightarrow Q = 4 \cdot 10^{-3} \text{ C} \quad \Rightarrow I = \omega Q \Rightarrow I = 1 \text{ A}$$

Άρα για $t=0$ $q=0$

Γ2.

συνεπώς

$$q = Q \sin \omega t$$

$$\text{για } t = \frac{T}{12} \quad q = Q \sin \frac{2\pi}{T} \frac{T}{12} \Rightarrow q = Q \frac{\sqrt{3}}{2}$$

$$\text{άρα } U_E = \frac{1}{2} \frac{q^2}{C} = \frac{1}{2} \frac{Q^2}{C} \frac{3}{4} \Rightarrow U_E = \frac{3}{4} E = 6 \cdot 10^{-2} \text{ J}$$

Γ3

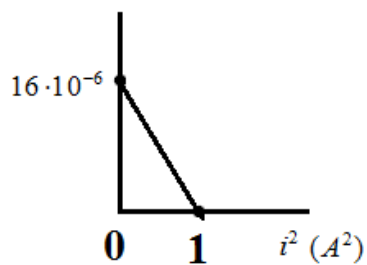
$$i = -\omega Q \cos \omega t \Rightarrow \frac{di}{dt} = -\omega^2 q$$

$$U_E = 3U_B \Rightarrow U_E = 3(E - U_E) \Rightarrow 4U_E = 3E \Rightarrow U_E = \frac{3}{4}E \Rightarrow q = \pm Q \frac{\sqrt{3}}{2}$$

$$\text{Άρα } \left| \frac{di}{dt} \right| = \omega^2 Q \frac{\sqrt{3}}{2} = 250 \frac{\sqrt{3}}{2} \text{ A/s} = 125\sqrt{3} \text{ A/s}$$

Γ4

Από Διατήρηση Ενέργειας ηλ.ταλάντωσης



$$U_E = E - U_B$$

$$\frac{1}{2} \frac{q^2}{C} = E - U_B \Rightarrow q^2 = 2 \cdot 10^{-4} \cdot 8 \cdot 10^{-2} (1 - i^2) \Rightarrow$$

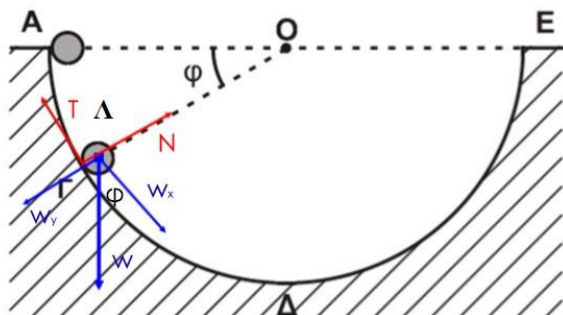
$$q^2 = 16 \cdot 10^{-6} - 16 \cdot 10^{-6} i^2 \quad SI$$

ή

$$\frac{1}{2} \frac{q^2}{C} - \frac{1}{2} Li^2 = \frac{1}{2} \frac{Q^2}{C} \Rightarrow q^2 = LC(1 - i^2) \Rightarrow$$

$$\Rightarrow q^2 = 16 \cdot 10^{-6} (1 - i^2)$$

ΘΕΜΑ Δ



Δ1.

$$\Sigma F_x = m \alpha_{cm(\Delta)} \Rightarrow mg \sin \phi - T_\sigma = m \alpha_{cm}$$

$$\Sigma \tau_\Delta = I_\Delta \alpha_\gamma \Rightarrow T_\sigma r = \frac{2}{5} m r^2 \alpha_\gamma \Rightarrow T_\sigma = \frac{2}{5} m r \alpha_\gamma$$

αλλά επειδή κάνει κύλιση χωρίς ολίσθηση έχουμε

$$r \cdot \alpha_\gamma = \alpha_{επιρ} = \alpha_{cm}$$

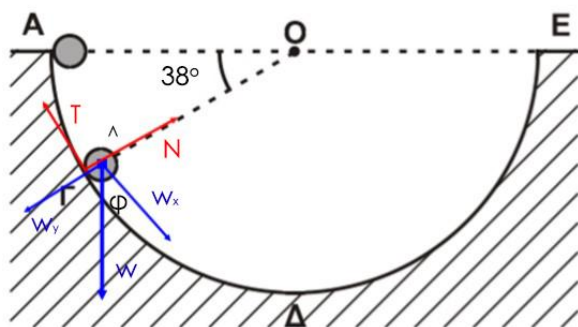
$$mg\sigma\upsilon\nu\phi - T_\sigma = m\alpha_{cm}$$

$$T_\sigma = \frac{2}{5}m\alpha_{cm}$$

$$mg\sigma\upsilon\nu\phi = \frac{7}{5}m\alpha_{cm} \Rightarrow \boxed{\alpha_{cm} = \frac{5}{7}g\sigma\upsilon\nu\phi}$$

$$\acute{\alpha}\rho\alpha T_\sigma = \frac{2}{5}m \frac{5}{7}g\sigma\upsilon\nu\phi \Rightarrow \boxed{T_\sigma = \frac{2}{7}mg\sigma\upsilon\nu\phi} = \frac{2}{7}1,4 \cdot 10\sigma\upsilon\nu\phi = 4\sigma\upsilon\nu\phi$$

Δ2.



$$\Lambda\Delta\text{ΜΕ: } K_\alpha + U_\alpha = K_\tau + U_\tau$$

$$mgh = \frac{1}{2}I_\Lambda\omega_1^2 + \frac{1}{2}mu_1^2$$

$$\eta\mu 30 = \frac{h}{R - \frac{R}{8}} = \frac{h}{\frac{7R}{8}} \Rightarrow h = \frac{7R}{8} \cdot \frac{1}{2} \Rightarrow \boxed{h = \frac{7R}{16}}$$

αλλά $u_1 = u_r = \omega r$

$$mg \frac{7R}{16} = \frac{1}{2} \frac{2}{5} mr^2 \omega_1^2 + \frac{1}{2} mu_1^2 \Rightarrow mu_1^2 = g \frac{7R}{16} = \frac{1}{5} mu_1^2 + \frac{1}{2} mu_1^2 \Rightarrow$$

$$\frac{7gR}{16} = \frac{7}{10} u_1^2 \Rightarrow u_1^2 = \frac{10gR}{16} \Rightarrow u_1 = \sqrt{\frac{10gR}{16}} = \sqrt{\frac{10 \cdot 10 \cdot 1,6}{16}} = \sqrt{10} \text{ m/s}$$

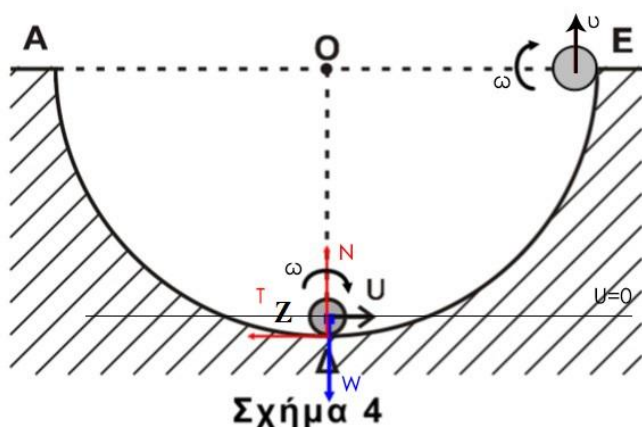
$$\text{Άρα } \Sigma F_{\text{ακτίνα ημισφαιρ.}} = m\alpha_{\kappa} = m \frac{u_1^2}{R - \frac{R}{8}} \Rightarrow N - w_y = \frac{mu_1^2}{\frac{7R}{8}} \Rightarrow$$

$$\Rightarrow N - mg\eta\mu 30 = \frac{m}{\frac{7R}{8}} \frac{10gR}{16} \Rightarrow N - \frac{mg}{2} = \frac{8m}{7R} \frac{10gR}{16} \Rightarrow$$

$$\Rightarrow N - \frac{mg}{2} = \frac{80mg}{7 \cdot 16} \Rightarrow N = \frac{mg}{2} + \frac{5}{7} mg \Rightarrow$$

$$\Rightarrow N = \frac{17mg}{14} \Rightarrow N = \frac{17 \cdot 1,4 \cdot 10}{14} \Rightarrow \boxed{N = 17N}$$

Δ3.



ΑΔΜΕ νέα σφαίρα:

$$K_a + U_a = K_\tau + U_\tau$$

$$\frac{1}{2}mu^2 + \frac{1}{2}I_z\omega^2 = \frac{1}{2}mu'^2 + \frac{1}{2}I_z\omega'^2 + mg\left(R - \frac{R}{8}\right)$$

$$\frac{1}{2}mu^2 + \frac{1}{2}\frac{2}{5}mr^2\omega^2 = \frac{1}{2}mu'^2 + \frac{1}{2}\frac{2}{5}mr^2\omega'^2 + mg\frac{7R}{8}$$

Ξέρω κάνει κύλιση χωρίς ολίσθηση

$$u' = u'_{\lambda\sigma} = \omega' r \text{ και } u = \omega r = u_{\gamma\rho}$$

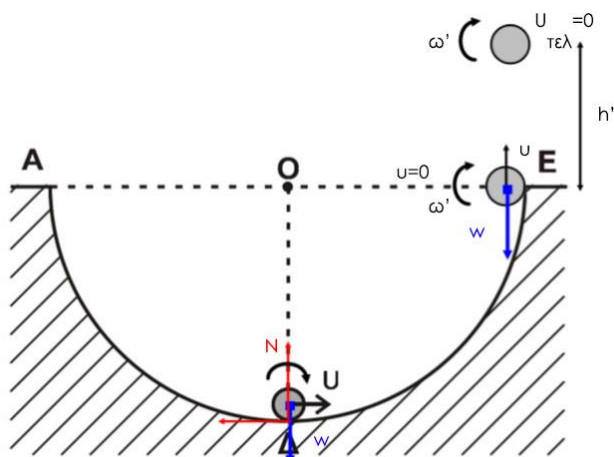
$$\frac{1}{2}u^2 + \frac{1}{5}u^2 = \frac{1}{2}u'^2 + \frac{1}{5}u'^2 + \frac{7gR}{8} \Rightarrow$$

$$\frac{7}{10}36 = \frac{7}{10}u'^2 + \frac{7 \cdot 10 \cdot 1,6}{8} \Rightarrow \frac{36}{10} = \frac{u'^2}{10} + 2 \Rightarrow$$

$$36 = u'^2 + 20 \Rightarrow u'^2 = 16 \Rightarrow u' = \sqrt{16} = 4 \text{ m/s}$$

$$\text{Άρα } u' = \omega' r \Rightarrow 4 = \omega' \cdot \frac{1,6}{8} \Rightarrow \omega' = \frac{4 \cdot 8}{1,6} \Rightarrow \omega' = 20 \text{ rad/s}$$

Η σφαίρα στο σημείο E εγκαταλείπει τον κύκλο άρα η μόνη δύναμη που επιδρά πλέον είναι το βάρος. Συνεπώς, αρχίζει ομαλά επιβραδυνόμενη μεταφορική αλλά και ομαλή στροφική.



Άρα ψηλότερο σημείο έχει $u_{\text{τελ}}=0$ αλλά το ω είναι ω'

ΑΔΜΕ

$$K_\alpha + U_\alpha = K_\tau + U_\tau \Rightarrow \frac{1}{2}mu'^2 + \frac{1}{2}I_z\omega'^2 = \frac{1}{2}mu_{\text{τελ}}^2 + \frac{1}{2}I_z\omega'^2 + mgh'$$

$$\Rightarrow \frac{1}{2}mu'^2 = mgh' \Rightarrow \frac{1}{2}16 = 10h' \Rightarrow \boxed{h' = 0,8 \text{ m}}$$

Δ4. Η μόνη δύναμη που επιδρά είναι το βάρος, που δεν προκαλεί ροπή

$$\frac{\Delta K_{\sigma\tau\rho}}{\Delta t} = P_{\sigma\tau\rho} = \Sigma \tau \cdot \omega' = \tau_w \omega' = 0 \quad \text{μόλις χάσει επαφή}$$

$$\text{άρα } \frac{\Delta L}{\Delta t} = \Sigma \tau = 0$$

Επιμέλεια: Αγγελής Γιάννης, Δοξόπουλος Κώστας, Μανελίδης Ν.